# FREE CONVECTION IN AN AIR-WATER VAPOR BOUNDARY LAYER

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Abstract-This paper describes an experimental investigation, supported by analysis, of free convection in an air-water vapor boundary layer at the stagnation point of a horizontal cylinder. A two-component boundary layer is created by the effusion of water vapor from the porous surface of the cylinder; the ambient gas is pure air. The results of both experiment and analysis indicate that the heat transfer decreases as the surface mass-transfer rate increases. At moderate blowing rates, there is good agreement between the experimentally- and analytically-determined Nusselt numbers. At higher mass-transfer rates, the data lie above the analytical predictions by about 25 per cent. This departure is attributed to a fluctuating motion in the boundary layer.

#### **NOMENCLATURE**

- g, acceleration of gravity;<br>h, heat-transfer coefficient
- 
- $h$ , heat-transfer coefficient;<br>*i*, specific enthalpy of stear specific enthalpy of steam;
- $k,$ thermal conductivity;
- $\dot{m}$ , mass-transfer rate/time-area;<br> $Nu$ . Nusselt number:
- Nusselt number:
- $q_{\text{cond}}$ , conductive heat flux;
- $q_{\text{rad}}$ , radiative heat flux;
- $q_w$ , convective heat flux;<br>r, cylinder radius;
- $r$ , cylinder radius;<br> $T$ , absolute temper
- absolute temperature;

 $W_{\text{H}_2\text{O}}$ , mass fraction of steam at surface.

### Greek symbols

- $\beta$ , coefficient of thermal expansion;
- $\epsilon$ , emittance;
- $\nu$ , kinematic viscosity;
- *P?* density;
- $\sigma$ , Stefan-Boltzmann constant.

## Subscripts

- aw, adiabatic wall;
- e, radiation environment;
- 0, interior of test section;
- w. cylinder surface ;
- $\infty$ . ambient air.

# **INTRODUCTION**

**BOUNDARY LAYER flows** involving mixtures of air

and water vapor may be found in many branches of technology. For instance, such flows may occur in the condensation of steam when air (a noncondensable) is present, in the humidification and dehumidification of air, and in a variety of chemical process operations. Recently, it has been suggested that the injection of steam through a porous surface into a hot air stream may be an effective means of surface thermal protection (i.e. mass-transfer cooling).

Upon consideration of the literature, it appears that such boundary layers have not yet been subjected to controlled experimental study. The present paper describes an experimental investigation, supported by analysis, of the airwater vapor boundary layer in a free-convection flow about a horizontal cylinder, The twocomponent boundary layer is created by passing steam from the interior of the cylinder out through pores in the cylinder surface; the cylinder is situated in an otherwise quiescent air environment. The measurements are concerned specifically with the heat-transfer characteristics at the stagnation point of the cylinder. These results are directly comparable to stagnationpoint solutions of the complete momentum, energy, and diffusion equations.

In the presentation that follows, a description will first be given of the experimental apparatus, with particular emphasis on the steam system.

Then, the data reduction procedure will be outlined. Next, the experimental results are presented, discussed and compared with those of analysis. Finally, additional analytical results will be given.

### **THE EXPERIMENTAL APPARATUS AND ITS OPERATION**

The description of the experimental apparatus is facilitated by reference to Fig. 1, which shows a schematic diagram of the main elements of the system. Saturated steam at approximately 300°F is generated in a boiler\* and passes through a pressure regulator and reducing valves to a superheater. The flow rate of the thus superheated steam is then measured by a calibrated orifice. Next, the steam passes through a second superheater which facilitates the adjustment of the test-section temperature. From the superheater, the flow enters the interior of the test section and then diffuses out through the porous wall into the boundary layer. All piping in the system was wrapped with fiberglass insulation.

The test section itself is a porous cylindrical shell, 3 inches in diameter and 12 inches in length. The shell is made of woven stainlesssteel cloth that consists of two layers of wovenwire mesh, bonded together by a sintering and rolling process. The thickness of the porous

\* Model ES 12, Automatic Steam Products Corporation.

wall is about 0.035 in. For purposes of support and isolation, the ends of the test cylinder are fitted with a pair of hollow Lucite cylinders, each 3 inches in diameter and 8 inches in length.

With a view toward achieving a uniform effusion of the steam through the surface, the stainless-steel shell is internally lined with an annulus of fiberglass filter paper of  $\frac{1}{2}$  in thickness. The steam is introduced into the interior of the test section through a  $\frac{1}{2}$  in diameter perforated tube that runs coaxially through the entire length of the porous cylinder.

Wall temperature measurements were accomplished with thermocouples welded to the inside surface of the porous shell. The thermocouple wire is iron-constantan, 36-gage. At the outset of the tests, there were a total of 40 such thermocouples, circumferentially distributed in a plane midway between the ends of the cylinder and in a pair of planes 2 in distant from the mid-plane. During the course of the experiment, many of the thermocouple junctions became inoperative due to the corrosive action of the steam.<sup>†</sup> Fortunately, a sufficient number of thermocouples in the stagnation region of the mid-plane continued operative throughout the entire duration of the tests. The temperature of the steam in the interior of the test section was sensed by thermocouples suspended in the

t The model had initially been designed to accommodate non-corrosive gases, and the thermocouple material was **chosen accordingly.** 



FIG. 1. The experimental apparatus.

openings of the delivery tube at several locations along its length. All thermocouple voltages were detected by a Brown Electronik selfbalancing potentiometer.

As indicated in Fig. 1, the test section is mounted horizontally in a hollow-walled cylindrical enclosure, 4 ft high and 2 ft in diameter. The bottom of the enclosure is partially closed with a circular plate, the primary function of which is to provide a known environment for radiant interchange with the lower stagnation region of the test section. The surface of the cylindrical enclosure and the end plate are both black. Thermocouples were affixed at various locations on the aforementioned surfaces. The air temperature at several positions within the cylindrical enclosure was sensed by shielded thermocouples.

In a further effort to achieve quiescent environmental conditions, the aforementioned cylindrical enclosure was housed in an enclosed space that is segregated by partitions from the remainder of the laboratory room. However, the partitions do not fully extend to the floor or to the ceiling; thus, air can be exchanged between the enclosed space and the room.

As was previously noted, the measurement of the steam flow rate is accomplished by employing a calibrated orifice. The orifice plate, fabricated according to ASME standards, has a hole diameter of  $\frac{1}{8}$  in and is situated in a tube of  $\frac{7}{16}$  in diameter. Pressure taps are located one diameter upstream and one-half diameter downstream of the orifice plate. Temperatures were also measured upstream and downstream of the orifice. The calibration was accomplished by ducting steam from the downstream end of the orifice section through a condenser. The condensate collected in a given period of time was weighed on a precision balance. It is believed that the orifice calibration is accurate to  $\pm 1$  per cent.

The measurement of the steam pressures upstream and downstream of the orifice was  $p_2$  sides of the manometer. This is the essential accomplished by employing a specially designed feature in the operation of the manometer. accomplished by employing a specially designed feature in the operation of the manometer.<br>manometer system. The manometer arrange-<br>Under this condition, it can readily be derived manometer system. The manometer arrange- Und<br>ment will now be discussed with the aid of that ment will now be discussed with the aid of Fig. 2. The pressures  $p_1$  and  $p_2$  respectively represent the upstream and downstream

pressure  $p_1 - p_2$ , one employs a U-tube as shown in the left-hand portion of the diagram. The top of each leg of the U-tube is connected to a separate glass chamber. Each chamber is



FIG. 2. Manometer system for measuring steam pressure.

partly filled with liquid water. The space above the water is filled with air, and the U-tube protrudes into the air space. The pressures  $p_1$  and  $p_2$  are conveyed to the respective chambers through horizontal copper tubes which are joined to glass tubes at the tops of the chambers. Under test conditions, the interface between the steam and the liquid water is located somewhere within the copper tube, both for the  $p_1$  and the  $p_2$  sides of the manometer. This is the essential

$$
p_1 - p_2 = \rho_{\rm Hg} g H_1 + \rho_{\rm H_2O} g h_1 \qquad (1)
$$

pressures.<br>For the measurement of the differential is illustrated in the right-hand portion of Fig. 2. is illustrated in the right-hand portion of Fig. 2. In this instance, one leg of the manometer is open to the atmosphere. Once again, the essential feature of the operation is that the interface between the steam and the liquid water be located in the horizontal copper tube. Correspondingly, one finds

$$
p_2 - p_{\infty} = \rho_{\rm Hg} g H_2 - \rho_{\rm H_2O} g h_2. \qquad (2)
$$

The U-tubes are approximately 60 inches in length. The glass chambers are  $1\frac{1}{2}$  inches in diameter and 3 inches long.

In carrying out the experiments, care had to be exercised to prevent condensation of steam in the test section. To this end, as a prelude to initiating the steam flow, hot air was passed through the system for about 1 h. At the end of this period, a temperature of 250-300°F was achieved in the test section. Then, the steam flow was actuated, and, after an additional period of 2 h, steadystate operation was achieved and data were collected.

Structural limitations of the apparatus precluded a wide range in the values of the wall temperature. For this reason and also to facilitate comparison with the analytical solutions (which contain as a parameter the ratio of wall temperature to environment temperature), it was deemed desirable to run all the tests at approximately a fixed wall temperature. Thus, the blowing rate of the steam is the principle independent variable of the experimental investigation. Analytical results are given for a range of thermal boundary conditions.

### REDUCTION OF DATA

The determination of the local heat-transfer rate at the stagnation point is accomplished by setting up an energy balance. In this connection, it is convenient to envision a control volume at the stagnation point that spans the porous steel shell and the fiberglass liner. Under steadystate conditions, the application of the energy conservation principle to such a control volume yields

$$
\dot{m} (i_o - i_w) = q_w + q_{\text{rad}} + q_{\text{cond}}.\tag{3}
$$

The left-hand side of this expression is the enthalpy change sustained by the steam as it passes from the interior of the test section to the surface. The symbols  $i_0$  and  $i_w$  represent the

enthalpy of steam in the interior and at the surface, while  $\dot{m}$  is the steam flow rate per unit surface area.

There are three heat-flux terms appearing on the right-hand side. The first of these,  $q_w$ , is the convective heat transfer from the wall to the boundary layer. The second is the net radiative transport between the porous shelf and the surroundings, while the last represents losses by heat conduction from the control volume. All heat fluxes are per unit surface area.

The enthalpy rise term is evaluated by employing the steam flow rate from the orifice and the temperatures  $T_0$  and  $T_w$  respectively measured in the interior of the model and on the porous stainless-steel shell. Typically,  $T_w$  was approximately 695°R (235°F), while  $T_0$  ranged from  $760^{\circ}R$  (300°F) to  $800^{\circ}R$  (340°F). The corresponding enthalpies<sup>\*</sup>  $i<sub>o</sub>$  and  $i<sub>w</sub>$  were read from the *Steam Tables* [l]. Tt is assumed that the steam emerging from the surface of the cylinder is at the same temperature as the stainless-steel shelf.

The net transport of radiation from the porous surface to the black-walled surroundings (temperature  $T_e$ ) is calculable from the relationship

$$
q_{\rm rad} = \epsilon \sigma \left( T_w^4 - T_e^4 \right) \tag{4}
$$

in which  $T_w$  is the measured temperature at the stagnation point and  $\epsilon$  is the surface emittance. From an independent experiment described in reference 2, it was determined that  $\epsilon = 0.407$ . Over the range of blowing rates of this investigation,  $q_{rad}$  ranged from 45 to 55 per cent of the enthalpy rise, with the higher values corresponding to higher blowing rates. Radiation contributions of this magnitude are altogether reasonable when free convection is the only alternate mode of heat transport.

The conduction losses were fully negligible in the present experiment, especially since consideration is being given to a thermally symmetric location such as the stagnation point.

In the light of the foregoing discussion, all terms of equation (3) except  $q_w$  are directly

<sup>\*</sup> In evaluating  $i_w$ , the partial pressure of the steam was taken from the analytical solutions that are discussed later.

evaluable from the measured data. Thus, *qw* can be determined from the difference between the enthalpy rise and the radiation flux. With the *qw*  values thus obtained, a local heat-transfer coefficient  $h$  is computed from the definition

$$
h = \frac{q_w}{T_w - T_\infty} \tag{5}
$$

The thermal driving force employed in the foregoing definition is  $(T_w - T_\infty)$ . In this connection, it may be noted that in two-component boundary layers, thermal diffusion effects may operate to create a condition whereby  $T_w \neq T_{\infty}$ when  $q_w = 0$  (see, for instance, reference 2). In such cases, an appropriate driving force is  $(T_w - T_{aw})$ , where  $T_{aw}$  is the adiabatic wall temperature (that is, the wall temperature corresponding to  $q_w = 0$ ).

For the air-water vapor boundary layer, analysis shows that the thermal diffusional effects are of secondary importance for the temperature differences and flow rates of this experiment. Moreover, owing to the onset of condensation, the adiabatic wall temperatures are not measureable. Additionally, the adiabatic wall temperatures predicted by analysis are prone to some uncertainty because the thermal diffusion factor is not known to within a factor of two [3]. In this light, it was deemed altogether reasonable to omit further consideration of the adiabatic wall temperature in the data reduction and to employ  $(T_w - T_\infty)$  as the thermal driving force.

The heat-transfer results are reported in terms of the dimensionless representation

$$
Nu\left/\sqrt{\left[\frac{r\left(gr\right)^{1}}{\nu_{\infty}}\right]},\quad Nu=\frac{hr}{k_{\infty}}\quad (6)
$$

where  $r$  is the cylinder radius and  $g$  is the acceleration of gravity. The particular form of the foregoing dimensionless grouping is suggested by analysis [4]. It may be observed that *(gr)'* has the dimensions of a velocity\*, and correspondingly,  $r(gr)^{\frac{1}{2}}/v_{\infty}$  is similar to a Reynolds number. A dimensionless mass injection parameter is also suggested by analysis

$$
-\frac{\dot{m}}{\rho_{\infty}(gr)^{\frac{1}{2}}}\sqrt{\left[\frac{r\left(gr\right)^{\frac{1}{2}}}{\nu_{\infty}}\right]}\tag{7}
$$

It is readily verified that the foregoing has the same form as the blowing parameter for forcedconvection mass-transfer cooling. In this investigation, *m* ranged from 4.1 to 7.8 lb/h ft<sup>2</sup>, and this resulted in a range of the mass injection parameter from 0.3 to 0.58.

### RESULTS AND DISCUSSION

The experimentally determined Nusselt numbers are plotted as open circles in Fig. 3 with



**FIG.** 3. Experimental and analytical heat-transfer results'

the dimensionless mass-transfer rate as independent variable. Also appearing in the figure is a solid line representing the prediction of analysis (the details of the analysis will be discussed later).

The experimental conditions were such that the ambient temperature  $T_{\infty}$  was approximately 535 $\mathrm{R}$  (75 $\mathrm{F}$ ). In the majority of the runs, the temperature ratio  $T_w/T_\infty$  had a value of 1.3. For three of the tests,  $T_w/T_\infty$  took on values between 1.31 and l-325. The Nusselt numbers for these points were corrected by l-2 per cent in accordance with theory. The experiments were performed under low-humidity environmental conditions, the mass fraction of water vapor in the environment being O-008 or less.

The analytical curve shown in the figure

<sup>\*</sup> The analysis takes account of variable fluid properties. Consequently, the factor  $\beta(T_w - T_\infty)$  does not naturally arise in the velocity grouping as for a constant property fluid.

corresponds to the thermal conditions

$$
T_{\infty} = 535^{\circ} \text{R} \text{ and } T_w/T_{\infty} = 1.3
$$

it was verified that this curve continues to apply tion on the mechanism of the fog formation. without perceptible change for cases in which the The analytical model does not take cognizance water vapor content of the environment is as of fog formation. much as 2 per cent (mass fraction). Furthermore, In view of Fig. 3, one may conclude that the within the scale of the figure this same curve fog layer did not have a first-order effect on the represents the heat-transfer results calculated heat-transfer results. However, it did serve quite both with and without the thermal diffusional effectively as an agent for flow visualization. effects. In the former case, the heat-transfer Thus, at low rates of mass transfer, the fog coefficient is defined with  $(T_w - T_{aw})$  as the film was seen to be basically stable, but with an thermal driving force; in the latter case, occasional lazy wave motion. At high mass-

effect of increased surface mass transfer is to quite plausible to the observer that such undecrease the convective Nusselt number. This steadiness could well augment the heat-transfer trend is consistent with prior experience with rates relative to those for a steady, laminar flow mass transfer cooling in forced-convection flows. pattern. However, as will be demonstrated later, the In light of the foregoing discussion, it may be opposite trend can sometimes occur in free- concluded that the analytical prediction can be convection flows. applied with confidence in the range of small

mental data scatter both above and below the of mass transfer, the analytical predictions analytical prediction. The extent of the scatter, appear to be conservative by about 25 per cent. which is about  $\pm 10$  per cent about a mean line, It should also be noted that stagnation-point is in no way excessive when it is recalled that the heat-transfer results apply without essential radiation correction amounts to approximately change in a substantial adjacent region on the 50 per cent of the overall heat-transfer rate. cylinder surface. Present measurements, as well It appears altogether reasonable to conclude that as those of prior investigations (e.g. reference 2), the analytical results are well confirmed by suggest that the stagnation point results can be experiment in the range of moderate blowing applied over a length of arc subtending  $45^\circ$  to rates. **Example 2** and the stagnation point. **each** side of the stagnation point.

At the higher mass-transfer rates, the data points show greater deviations from the analytical curve. As will be developed in the forthcoming discussion, these deviations are attributable to departures of the operating conditions from the steady, laminar flow postulated in the analysis.

During the course of the experiments, visual observations of the up-facing portion of the test section were made from a suitably arranged platform. For all operating conditions, one could see the following: adjacent to the porous surface, there was a clear layer of gas; farther from the surface, a layer containing fog particles was in evidence. Such a fog layer was observed for all the blowing rates investigated. Moreover, it was present during the final runs (performed

under low-humidity conditions) as well as during preliminary runs performed under highhumidity conditions. At the present time, the and to an ambient gas that is pure air. However, authors are unable to provide further informa-

 $(T_w - T_\infty)$  is used as the thermal driving force. transfer rates, the oscillations of the fog layer Inspection of the figure indicates that the were stronger and more frequent. It appeared

At the lower mass-transfer rates, the experi- and moderate mass-transfer rates. At higher rates

It may be of interest to consider the concentrations of water vapor at the cylinder surface that correspond to the mass-transfer rates of the present investigation. This information has been determined from the aforementioned analytical solutions and is presented in the lower portion of Fig. 4 as the curve corresponding to  $T_w/T_\infty = 1.3$ . The ordinate  $W_{\text{H}_2\text{O}}$  is the mass fraction of water vapor at the cylinder wall, while the abscissa is the mass-transfer parameter. Inspection of the figure reveals that the water vapor concentration increases with increasing mass transfer rate. For the range of masstransfer rates of this investigation, the mass fraction of water vapor ranges from  $0.52$  to  $0.78.$ 



FIG. 4. Analytical results for a range of thermal boundary conditions.

# *Additional analytical results*

The analytical results alluded to in the foregoing section of the paper are based on solutions of the complete momentum, energy, and diffision equations. The boundary-layer approximations were not utilized. The practicability of dealing with the complete conservation equations is one of the attractive features of working with stagnation-point flows.

The analytical formulation of the problem follows the same lines as was discussed in reference 4 for the helium-air free-convection boundary layer. Consequently, to conserve space, the governing equations will not be repeated here. A necessary ingredient for the solution of these equations is a knowledge of the thermodynamic and transport properties of air, water vapor, and mixtures thereof. The properties of pure air are well documented for the temperature range of this investigation. However, the transport properties of steam and in particular, of air-steam mixtures, are somewhat uncertain. The latter properties were taken from a very recent paper by Mason and Monchick **[31.** 

The numerical solution of the governing conservation equations is a formidable undertaking, even for a high-speed digital computer. This is because of the lengthy and complex representations of the fluid properties and of the intercoupling between the governing equations. The numerical work was performed on a Control Data 1604 computer at the Numerical Analysis Center of the University of Minnesota.

The analytical results thus obtained are presented in Fig. 4. The upper part of the figure pertains to the Nusselt number. The solid lines in the lower portion of the figure provide

information on the mass fraction of water Within the scale of the figure, the same curves vapor at the cylinder surface; the dashed curve for Nu and  $W_{H<sub>20</sub>}$  represent results from two gives results for the adiabatic wall temperature different sets of solutions; in one set, the thermal which is created by thermal diffusional effects. diffusional effects have been fully included, These results are plotted as a function of the while in the other set, these diffusional effects mass-transfer parameter for parametric values were suppressed. In the former case, the heatof  $T_w/T_\infty$ . The environment temperature is transfer coefficient is defined with  $(T_w - T_{aw})$  $535^\circ$ R; however, the results are quite insensitive as the thermal driving force; while in the latter, to the value of  $T_{\infty}$  over a moderate range.  $(T_w - T_{\infty})$  is the thermal driving force.

is seen that the Nusselt numbers generally sented in the bottom portion of the figure show decrease with increasing mass-transfer rate. a much smaller departure from unity than was This is due to the thickening of the boundary previously found for injection of light gases such layer that results from mass injection. However, as helium and hydrogen [2,4]. Moreover, these the aforementioned trend is reversed at small results are of somewhat uncertain accuracy

that there are two opposing effects of the surface water vapor mixtures. mass transfer. One of these is to thicken the boundary layer. The other is to augment the CONCLUDING REMARKS buoyancy force by adding a light-weight com- The general good agreement between analysis ponent to the boundary layer. When the and experiment in the range of moderate blowing temperature differences of the problem are rates has interesting implications in the theory of sufficiently large, the temperature-induced buoy- mass transfer cooling. This is because in this ancy force overshadows the concentration-in- range, analysis for forced-convection flows duced buoyancy force. However, when the [5,6] predicts that water vapor is a better mass temperature differences are relatively small, the transfer coolant than is helium. This is in concentration-induced buoyancy may augment contradistinction to the simple rule that arranges the velocities of the problem so as to cause an the effectiveness of a coolant gas according to its increase in heat transfer. This increase persists molecular weight, the effectiveness being greater only until the thickening effect of the surface at lower molecular weights. mass transfer takes over.

The molecular weight of water vapor is only<br>
coderately different from that of air Conse-<br>
The research described herein was supported by a moderately different from that of air. Conse-<br>grant from the U.S. Air Force Office of Scientific Re-<br>grant from the U.S. Air Force Office of Scientific Requently, the effects of the concentration-induced buoyancy are much smaller than those associated with the injection of a very light gas such as to Mr. W. J. Minkowycz for assistance with the computer helium. The minor role of the concentration- operations. helium. The minor role of the concentrationinduced buoyancy in the case of steam injection<br>is further exemplified by the appreciable spread  $\frac{1}{1}$  H KENNAN and E. G KE among the Nusselt number curves of Fig. 4 as a *Properties of Steam*. John Wiley, New York (1946).<br>function of the temperature ratio  $T_{eq}/T_{eq}$ . On 2. E. M. Sparrow, C. J. Scorr, R. J. Forstrom and function of the temperature ratio  $T_w/T_\infty$ . On <sup>2</sup>. E. M. SPARROW, C. J. SCOTT, R. J. FORSTROM and the other hand for the case of helium injection W. A. EBERT, Experiments on the diffusion-thermo the other hand, for the case of helium injection, corresponding Nusselt number results show only a weak dependence on the temperature ratio [4].

at the surface,  $W_{\text{H}_2\text{O}}$ , increases with increasing mass-transfer rate. At a given value of the masstransfer parameter, larger values of  $W_{\text{H}_2\text{O}}$ correspond to smaller values of  $T_w/T_\infty$ .

Upon considering the heat-transfer results, it The adiabatic wall temperature ratios preblowing rates for  $T_w/T_\infty = 1.1$ . owing to appreciable uncertainties in the magni-To illuminate this finding, it may be observed tudes of the thermal diffusion factor for air-

search, Mechanics Division. The authors are indebted to Professor E. R. G. Eckert for incisive discussion, and

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Résumé--Cet article décrit une étude expérimentale, confirmée par la théorie, de la convection naturelle dans une couche limite d'un mélange d'air et de vapeur d'eau au point d'arrêt d'un cylindre circulaire. La couche limite à deux constituants est créée par l'effusion de la vapeur d'eau à partir de la surface poreuse du cylindre; le gaz ambiant est de l'air pur. Les résultats de l'expérience et de la theorie indiquent tous les deux que le transport de chaleur diminue lorsque la vitesse du transport de masse à la paroi augmente. A des vitesses de soufflage modérées, il y a un bon accord entre les nombres de Nusselt determines experimentalement et par la theorie. A des vitesses de transport de masse plus élevées, les données expérimentales se trouvent environ à 25 % au-dessus des prévisions théoriques. Cet écart est attribué à un mouvement fluctuant dans la couche limite.

Zusammenfassung-Für freie Konvektion in einer Luft-Wasserdampf Grenzschicht am Staupunkt eines waagerechten Zylinders wird eine experimentelle Untersuchung zusammen mit einer Analyse beschrieben. Die zwei-Komponenten Grenzschicht wird durch Austreten von Wasserdampf aus der porösen Zylinderoberfläche erzeugt; das umgebende Gas ist reine Luft. Die Ergebnisse sowohl des Experiments als such der Analyse zeigen, dass der Warmetibergang abnimmt wenn der Stofftibergang an der Oberflache zunimmt. Für geringe Austrittsgeschwindigkeiten herrscht gute Übereinstimmung zwischen den experimentell und analytisch ermittelten Nusseltzahlen. Bei hohreren Stoffstromdichten liegen die Versuchsergebnisse etwa 25% tiber den analytischen Voraussagen. Diese Abweichung wird einer fluktuierenden Bewegung in der Grenzschicht zugeschrieben.

**Аннотация**—В статье описывается экспериментальное исследование вместе с расчетами свободной конвекции в пограничном слое воздухводяной пар в критической точке горизонтального цилиндра. Двухсоставной пограничный слой создается эффузией водяного пара из пористой поверхности цилиндра; окружающим газом является чистый воздух. Экспериментальные и расчетные результаты показывают, что теплообмен уменьшается с увеличением скорости теплообмена на поверхности. При не слишком больших скоростих сдувания найдено хорошее соответствие между числами Нуссельта, полученными экспериментально и теоретически. При более высоких скоростях теплообмена опытные данные превышают аналитические расчеты примерно на  $25$  процентов. Это отклонение объясняется флуктуациями в пограничном слое.